Charged jet cross section and fragmentation in proton-proton collisions at $\sqrt{s} = 7$ TeV

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Charged jet cross section and fragmentation in proton-proton collisions at $\sqrt{s} = 7$ TeV

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We report the differential charged jet cross section and jet fragmentation distributions measured with the ALICE detector in proton-proton collisions at a center-of-mass energy $\sqrt{s} = 7$ TeV. Jets with pseudorapidity $|\eta| < 0.5$ are reconstructed from charged particles using the anti-$k_T$ jet-finding algorithm with a resolution parameter $R = 0.4$. The jet cross section is measured in the transverse momentum interval $5 \leq p_T^{ch\text{jet}} < 100$ GeV/$c$. Jet fragmentation is studied measuring the scaled transverse momentum spectra of the charged constituents of jets in four intervals of jet transverse momentum between 5 and 30 GeV/$c$. The measurements are compared to calculations from the PYTHIA model as well as next-to-leading-order perturbative QCD calculations with POWHEG+PYTHIA8. The charged jet cross section is well described by POWHEG for the entire measured range of $p_T^{ch\text{jet}}$. For $p_T^{ch\text{jet}} > 40$ GeV/$c$, the PYTHIA calculations also agree with the measured charged jet cross section. PYTHIA6 simulations describe the fragmentation distributions to 15%. Larger discrepancies are observed for PYTHIA8.

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1. INTRODUCTION

The measurement of jets in proton-proton (pp) collisions allows the study of hard scatterings and subsequent fragmentation of partons (quarks and gluons). In this work, measurements of the charged jet cross section and jet fragmentation in pp collisions at $\sqrt{s} = 7$ TeV are presented. The inclusive charged jet cross section is measured in the transverse momentum ($p_T$) range $5 \leq p_T^{ch\text{jet}} < 100$ GeV/$c$. For sufficiently high $p_T$, jet production cross sections can be calculated in perturbative quantum chromodynamics (pQCD) supplemented with parton distribution functions (PDFs), assuming collinear factorization. Soft processes (e.g., production of particles or prompt photons with $p_T \lesssim 2$ GeV/$c$ [1–3]) cannot be described by this formalism. The measurements presented in this paper test the applicability of pQCD on jet production [4] down to a kinematic regime of the order of a few GeV/$c$ and provide experimental constraints on the PDFs (see e.g., Ref. [5]). Quantitative pQCD predictions for the charged jet cross sections are obtained in the POWHEG [6–8] scheme, in which matrix elements are calculated at next-to-leading order (NLO) in the QCD coupling and matched to parton shower Monte Carlo (MC) event generators to simulate parton fragmentation.

In Ref. [2], it was found that NLO pQCD overestimates the measured cross sections for inclusive $p^0$ and $\eta$ meson production at $\sqrt{s} = 7$ TeV. Perturbative QCD calculations of hadron production rely strongly on parton to hadron fragmentation functions [9], whereas for jet observables this dependence is much smaller. The measured charged jet cross sections help to trace the origin of this observed discrepancy.

The production cross sections of jets in pp collisions at $\sqrt{s} = 7$ TeV were measured previously by the ATLAS Collaboration for $100 \leq p_T^{jet} < 2000$ GeV/$c$ [10] and in the charged jet $p_T$ range $4 \leq p_T^{ch\text{jet}} < 100$ GeV/$c$ [11] and by the CMS Collaboration for $18 \leq p_T^{jet} < 1100$ GeV/$c$ [12] and $100 \leq p_T^{jet} < 2000$ GeV/$c$ [13]. Jet fragmentation in pp and Pb-Pb collisions at the LHC were reported by ATLAS [11,14,15] and CMS [16]. In Ref. [17], the ALICE Collaboration measured charged jet cross sections and leading jet properties for $20 \leq p_T^{ch\text{jet leading}} < 100$ GeV/$c$. An approximate scaling of the fragmentation distributions with the fractional transverse momentum $z^{ch} = p_T^{\text{particle}}/p_T^{ch\text{jet}}$ was observed for $z^{ch} > 0.1$ and the distributions were found to be similar for the reported $p_T^{ch\text{jet leading}}$ range. The results presented in this work repeat the previous measurements for a jet resolution parameter of anti-$k_T$ [18] jets with $R = 0.4$ with smaller uncertainties and an extended jet $p_T$ coverage. The distributions of the fractional transverse momentum $z^{ch}$

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of particles in jets with $5 \leq p_T^{ch,jet} < 30$ GeV/$c$ presented in this work test the fragmentation scaling for lower jet $p_T$. Furthermore, they provide constraints on the parton shower and hadronization models in MC event generators in a kinematic regime where strong nonperturbative effects are expected. In commonly used event generators, soft particle production is modeled by hard parton fragmentation and multiparton interactions, evoking nonperturbative color reconnection [19,20] at hadronization.

The present results allow the perturbative contribution to inclusive particle production to be quantified and also allow for tests of color reconnection effects on the fragmentation of jets with $p_T^{ch,jet} > 5$ GeV/$c$.

This paper is organized as follows. Section II describes the experiment and detectors used for these measurements. The observables and the details of the jet reconstruction algorithms and parameters are discussed in Sec. III. Section IV discusses the MC simulations carried out for comparisons of data to models, corrections for instrumental effects, and systematic uncertainty studies. The procedures applied to correct for instrumental effects are described in Sec. V. The methods used to evaluate the systematic uncertainties of the measurements are discussed in Sec. VI. Results are presented and discussed in comparison with MC event generator simulations in Sec. VII. Section VIII summarizes the results and conclusions.

II. EXPERIMENTAL SETUP AND DATA SAMPLE

The data used in this analysis were collected during the 2010 LHC pp run with the ALICE detector [21]. The analysis relies primarily on the time projection chamber (TPC) [22], the inner tracking system (ITS) [23], and the V0 [24] subdetectors. The V0 and ITS are used for event selection. The results reported in this paper are based on $177 \times 10^6$ minimum bias events corresponding to an integrated luminosity of $(2.9 \pm 0.1)$ nb$^{-1}$ [25]. The minimum bias trigger requires at least one hit in either the V0 forward scintillators or in the two innermost silicon pixel detector layers (SPD) of the ITS, in coincidence with a LHC bunch crossing. The TPC and ITS are used for primary vertex and track reconstruction. Only events with a primary vertex within $\pm 10$ cm along the beam direction from the nominal interaction point are analyzed to minimize dependencies of the TPC acceptance on the vertex position.

Charged tracks are reconstructed using the combined information from the TPC and the ITS within $|\eta| < 0.9$ over the full azimuth ($\phi$). The track selection criteria are the same as described in Ref. [17] and are briefly outlined here. To assure a uniform $\phi$ distribution, a hybrid reconstruction technique is utilized, combining two distinct track classes: (i) tracks containing from three to six hits in the ITS, including at least one hit in the SPD, and (ii) tracks containing fewer than three hits in the ITS, or no hit in the SPD. The momentum of tracks of class (i) is determined without a vertex constraint. The vertex constraint is added for class (ii) tracks to improve the determination of their transverse momentum. The track momentum resolution $\sigma_{p_T}/p_T$ is approximately 4% at $p_T = 40$ GeV/$c$ for 95% of all tracks. For tracks without a hit in the ITS (5% of the track sample) the resolution is 7% at $p_T = 40$ GeV/$c$.

Tracks from primary particles are selected requiring a minimum distance of closest approach to the primary vertex of 2.4 cm in the plane transverse to the beam and 3.2 cm in the beam direction.

To ensure good momentum resolution, tracks in the TPC are selected requiring a $p_T$-dependent minimum number of space points and a maximum $\chi^2$ to ensure track fit quality. In addition, there is an upper threshold on the $\chi^2$ of the results of the track fit using all the space points in the ITS and TPC, and using only the TPC space points with the primary vertex position as an additional constraint.

The track reconstruction efficiency for primary charged particles is approximately 60% at $p_T = 0.15$ GeV/$c$, about 87% at 1 GeV/$c$, and is nearly uniform up to 10 GeV/$c$ beyond which it decreases slightly. The efficiency is roughly uniform in azimuth and within the pseudorapidity range $|\eta| < 0.9$. Further details on the track selection procedure and tracking performance can be found in Refs. [17,26].

III. JET RECONSTRUCTION AND OBSERVABLES

The anti-$k_T$ [18] algorithm from the FASTJET package [27] is used for charged jet reconstruction. Jets with a resolution parameter $R = 0.4$ are reconstructed from charged tracks with $p_T > 0.15$ GeV/$c$ and within $|\eta| < 0.9$. The analyses reported in this work are restricted to jets detected within the fiducial acceptance $|\eta| < 0.5$. A boost-invariant $p_T$ recombination scheme is used to determine the transverse momenta of jets as the sum of their charged particle transverse momenta.

The cross section is evaluated with

$$\frac{d^2\sigma^{ch,jet}}{dp_T d\eta}(p_T^{ch,jet}) = \frac{1}{L_{int}} \frac{\Delta N_{jets}}{\Delta p_T \Delta \eta} (p_T^{ch,jet}), \quad (1)$$

where $L_{int}$ is the integrated luminosity and $\Delta N_{jets}$ is the number of jets in the selected intervals of $\Delta p_T$ and $\Delta \eta$.

The jet fragmentation is reported based on the distribution

$$F(z^{ch}, p_T^{ch,jet}) = \frac{1}{N_{jets}} \frac{dN}{dz^{ch}}, \quad (2)$$

where $N$ is the number of charged particles. The scaled $p_T$ variable $z^{ch}$ is calculated jet by jet for each track.
This observable characterizes the longitudinal jet fragmentation parallel to the jet axis.

IV. MONTE CARLO SIMULATIONS

Simulations of the ALICE detector performance for particle detection and jet reconstruction are used to correct the measured distributions for instrumental effects, evaluate systematic uncertainties, and make model comparisons to data. The simulated and real data are analyzed with the same reconstruction algorithms. The nominal corrections are calculated from simulated events generated with the PYTHIA 6.425 [28] (tune Perugia-0 [29]) MC model and particles are transported with GEANT3 [30]. The MC models HERWIG 6.510 [31,32] and several PYTHIA6 tunes are used for systematic investigations of the sensitivity of the MC correction factors to variations of the detector response (described in Sec. V) as well as to jet fragmentation and hadronization patterns (as described in Secs. VI A and VI B). For comparison to data in Sec. VII, PYTHIA6, PYTHIA8 [33], and POWHEG+PYTHIA8 simulations are used.

PYTHIA and HERWIG are leading-order (LO) event generators based on pQCD calculations of (2 → 2) hard scattering elements. Higher-order emissions are included in the parton shower. PYTHIA and HERWIG utilize different approaches to describe the parton shower and hadronization processes. HERWIG makes angular ordering a direct part of the evolution process and thereby takes coherence effects into account in the emission of soft gluons. PYTHIA6.4 is based on transverse-momentum-ordered showers [34] in which angular ordering is imposed by an additional veto. In PYTHIA6 the initial-state evolution and multiple parton-parton interactions are interleaved into one common decreasing \( p_T \) sequence. In PYTHIA8 the final-state evolution is also interleaved with initial-state radiation and multiparton interactions. Hadronization in PYTHIA proceeds via string breaking as described by the Lund model [35], whereas HERWIG uses cluster fragmentation. The PYTHIA Perugia tune variations, beginning with the central tune Perugia-0 [29], are based on LEP, Tevatron, and SPS data. The PYTHIA6 Perugia-2011 family of tunes [29] belongs to the first generation of tunes that use LHC pp data at \( \sqrt{s} = 0.9 \) and 7 TeV. For the PYTHIA8 Monash tune [36] data at \( \sqrt{s} = 8 \) and 13 TeV are also used. The HERWIG generator version and PYTHIA tunes used in this work utilize the CTEQ6L parton distributions [5]. The PYTHIA8.21 Monash tune uses the NNNPDF2.3 LO set [37].

The POWHEG BOX framework [7,8], an event-by-event MC, was used for pQCD calculations of (2 → 2) and (2 → 3) parton scattering at \( O(\alpha_s^3) \) in the strong coupling constant. The outgoing partons from POWHEG are passed to PYTHIA8 event by event where the subsequent parton shower is handled. The MC approach has the advantage that the same selection criteria and jet finding algorithm can be used on the final-state particle level as used in the analysis of the real data; in particular, charged particles can be selected. For the comparison with the measured differential jet cross sections, the CTEQ6M parton distribution functions [38] are used [39]. The dominant uncertainty in the parton-level calculation is given by the choice of renormalization scale, \( \mu_R \), and factorization scale, \( \mu_F \). The default value was chosen to be \( \mu_R = \mu_F = p_T \) of the underlying Born configuration, here a QCD 2 → 2 scattering [8]. Independent variations by a factor of 2 around the central value are considered as the systematic uncertainty. In addition, the uncertainty on the parton distribution functions has been taken into account by the variation of the final results for the respective error sets of the PDFs. For the POWHEG calculations, PYTHIA8 tune Monash was used. For test purposes, the calculations were repeated with multiparton interactions (MPI) switched off as an alternative setting.

V. CORRECTIONS

The measured jet spectra and fragmentation distributions are corrected to the primary charged particle level, as discussed in the following sections.

A. Unfolding

Momentum-dependent imperfections in the particle detection efficiency and the finite track momentum resolution of the detector affect the jet energy scale and jet fragmentation distributions reported in this work. A detector response matrix is used to correct the jet spectra and fragmentation distributions for these effects. The instrumental response is modeled in a full simulation of the ALICE detector. Simulated events are generated with PYTHIA and the produced particles are transported with GEANT3. Jets are reconstructed both directly from the charged particle momenta produced by the MC generators (particle level) and from the generator outputs processed through GEANT and the ALICE reconstruction software (detector level).

The jet production cross sections and fragmentation distributions are corrected by one- and two-dimensional Bayesian unfolding [40], respectively, as implemented in the RooUNFOLD [41] software. For the unfolding of the jet cross sections, a two-dimensional response matrix of particle-level versus detector-level charged jet \( p_T \) is used. The entries of the response matrix are computed pairing particle- and detector-level jets geometrically, according to the distance \( d = \sqrt{\Delta \eta^2 + \Delta \phi^2} \) between the jet axes. A bijective match with \( d < 0.3 \) is required. At the smallest jet \( p_T \) presented in this work, \( p_T^{ch,jet} = 5 \) GeV/c, the combined efficiency of jet reconstruction and matching detector- and particle-level jets exceeds 95%, and rises as a function of \( p_T^{ch,jet} \) to reach a value \( >99\% \) at \( p_T^{ch,jet} = 20 \) GeV/c. The fragmentation distributions are corrected with a four-dimensional response matrix with the axes corresponding to particle- and detector-level charged jet \( p_T \).
and particle- and detector-level $z^{ch}$, respectively. Particle-level and detector-level jet constituents used in the calculation of $z^{ch}$ are associated by matching the simulated TPC clusters on tracks to hits along the particle trajectories.

In the Bayesian approach, the unfolding solution is regularized by the choice of the number of iterations. We observe that the unfolded distributions typically converge to a solution after five steps. To avoid biases for the lowest and highest values of jet $p_T$ reported in this paper, a wide range $0 < p_T^{ch,jet} < 200 \text{ GeV/c}$ is chosen for the uncorrected distributions. Consistency of the unfolding procedure is ensured by folding the solution to the detector level and comparing it to the uncorrected distribution used as input. As an additional cross-check, the analysis of charged jet cross sections is also carried out with the RooUNFOLD implementation of the singular value decomposition unfolding technique [41,42]. Consistent results are obtained with both methods.

The requirement of a match between the simulated detector- and particle-level jets used to compute the response matrix introduces a kinematic bias towards higher momentum constituents. The effect is largest for the fragmentation distribution observable, where it is of the order of 5% for small values of $z^{ch}$ and $5 \leq p_T^{ch,jet} < 10 \text{ GeV/c}$. The bias decreases for higher values of $z^{ch}$ and $p_T^{ch,jet}$. For the jet cross section observable it is less than 0.5%. We account for this effect by applying a correction to the measured distributions prior to unfolding. The correction and the unfolding procedure are validated by MC closure checks, which will be discussed in Sec. VI.

B. Contamination from secondary particles

Secondary charged particles are produced by weak decays of strange particles (e.g., $K^0_S$ and $\Lambda$), decays of charged pions, conversions of photons from neutral pion decays and hadronic interactions in the detector material. Although the contribution of secondaries is minimized by the track selection described in Sec. II, the measured distributions nonetheless must be corrected for a small residual contamination.

The correction for secondary particle contamination is implicitly included in the unfolding of the measured cross sections. It is however carried out separately and explicitly prior to unfolding in the measurements of the fragmentation function, following the procedure described in Ref. [17]. The contribution of secondaries is estimated from MC simulations, separately for each bin in jet $p_T^{ch,jet}$ and particle $z^{ch}$. The explicit subtraction allows for the enhancement of the low strangeness yield in the PYTHIA Perugia-0 simulations to the level observed in data. Strange particle production in non-single-diffractive events by the CMS Collaboration [43] and MC simulations from Refs. [44,45] are compared. The MC predictions are scaled up to match the data. The contamination of secondaries from strange particle decays is small, and the effect of the strangeness scaling on the final result is less than 1%.

C. Underlying event subtraction

The underlying event (UE) corresponds to all particles in an event that are not produced directly by the hard scattering of partons. UE particles emitted in the jet cone contribute to the reconstructed jet $p_T$. To estimate and subtract the UE activity, we use the approach discussed in Ref. [17]. The UE particle yield is measured event by event based on circular regions transverse to the axis of the leading (highest $p_T$) jet. The circular regions have the same radius as the jet resolution parameter and are placed at the same pseudorapidity as the leading jet but offset at an azimuthal angle $\Delta \phi = \pi/2$ relative to the jet axis. For the jet cross section measurements, the UE is subtracted on a jet-by-jet basis prior to unfolding. The relative UE contribution to the total measured jet $p_T$ is largest for the soft jets. The correction results in a reduction of the uncorrected jet yield by approximately 25% for $p_T^{ch,jet} = 5 \text{ GeV/c}$ and by about 10% for $p_T^{ch,jet} = 20 \text{ GeV/c}$.

The method used in Ref. [17] to correct the fragmentation distributions in jets with $p_T^{ch,jet,leading} \geq 20 \text{ GeV/c}$ for the UE applies a subtraction on the level of the constituent spectra, but does not include a simultaneous correction to $p_T^{ch,jet}$. For low-$p_T$ jets, this approximation may not be valid. Therefore, in this work the fragmentation distributions are presented without correction for the UE.

VI. SYSTEMATIC UNCERTAINTIES

A summary of all systematic uncertainties for the cross section and fragmentation measurements is given in Table I for selected bins in $p_T^{ch,jet}$ and $z^{ch}$ to illustrate the range of systematic uncertainties.

A. Tracking efficiency and resolution

Uncertainties associated with the momentum resolution and charged track reconstruction efficiency lead to systematic uncertainties in measurements of the jet cross section and jet fragmentation distributions. The relative systematic uncertainty on tracking efficiency is estimated to be 4% based on variations of track selection criteria. The track momentum resolution has a relative systematic uncertainty of 20% [46].

The impact of the finite detector efficiency and momentum resolution on the unfolded jet cross sections and fragmentation distributions is estimated by applying a parametrized detector response to PYTHIA events clustered with FASTJET. The efficiency and resolution are varied independently, and a response matrix is computed for each variation. The measured distributions are unfolded, and the resulting variations are used to estimate the systematic uncertainties. The systematic uncertainty on the jet cross
sections related to tracking efficiency increases smoothly with increasing $p_T^{\text{ch jet}}$. For the fragmentation distributions, the uncertainty is largest at $z^{\text{ch}} = 1$ and has a minimum at $z^{\text{ch}} \approx 0.35$. The systematic uncertainty on the measured cross sections and fragmentation distributions from finite momentum resolution is comparatively small, and largest for high $p_T^{\text{ch jet}}$ and $z^{\text{ch}}$.

### B. Unfolding

The data correction methods used in this work are largely based on tune Perugia-0 of the PYTHIA event generator. The particular structure of jets simulated by PYTHIA might however affect the simulated detector response and influence the correlation between particle- and detector-level quantities used to compute the response matrices. Furthermore, the RooUNFOLD Bayesian unfolding algorithm is based on a prior solution which is initially obtained from the MC and updated in subsequent iterations. The choice of a particular initial prior might have an impact on the unfolded solution. Such event generator dependencies are examined by comparing unfolded solutions obtained with response matrices from the PYTHIA tunes Perugia-0 and Perugia-2011 with those obtained with the HERWIG generator. This is accomplished with a parametrized detector response and the anti-$k_T$ jet finder. The resulting systematic uncertainties on the jet cross sections are largest for the lowest $p_T^{\text{ch jet}}$. For the fragmentation distributions, the strongest event generator dependence is observed for the lowest jet $p_T$, in the interval $5 \leq p_T^{\text{ch jet}} < 10 \text{ GeV/c}$, where the uncertainty is largest for intermediate values of $z^{\text{ch}} \approx 0.4$ and for $z^{\text{ch}} = 1$. The distributions for $p_T^{\text{ch jet}} \geq 10 \text{ GeV/c}$ show a monotonic increase of the systematic uncertainty with $z^{\text{ch}}$.

The unfolding approach is validated by closure tests on PYTHIA simulations. To detect potential biases, the simulated detector-level distribution is unfolded and the solution is compared to the particle-level truth. For the unfolded jet cross section, no significant difference is observed. For the fragmentation distributions, a small systematic bias can be detected. We assign a constant uncertainty of 1% to account for this nonclosure.

### C. Correction for secondary charged particles

The systematic uncertainty associated to the correction for the contribution from secondary charged particles to the jet cross sections and fragmentation distributions is estimated by varying track selection criteria. We change the contribution of secondary charged particles by varying the track selection criteria [17] and correct the measured distributions accordingly. Residual variations of the corrected distributions are used to estimate the systematic uncertainties. The resulting uncertainties on the fragmentation distributions are largest at small values of $z^{\text{ch}}$. The uncertainty on the measured jet cross section is evaluated as a $p_T^{\text{ch jet}}$ scale uncertainty of 0.5%.

### D. Underlying event subtraction

The jet cross sections are corrected for the contribution from the UE. In Ref. [17], the uncertainty on the measurement of the UE $p_T$ density was estimated to be 5%. The corresponding uncertainty of the jet cross section is evaluated as a jet $p_T$ scale uncertainty resulting in a systematic uncertainty which is 2% for $p_T^{\text{ch jet}} = 5 \text{ GeV/c}$ and decreases for higher $p_T^{\text{ch jet}}$.

### VII. RESULTS

Figure 1 presents the inclusive charged jet cross section measured in pp collisions at $\sqrt{s} = 7 \text{ TeV}$ using the anti-$k_T$ jet finder. The cross section is reported for a resolution parameter $R = 0.4$ in the pseudorapidity interval $|\eta| < 0.5$. Statistical uncertainties are displayed as vertical error bars. The total systematic uncertainties are obtained as a quadratic sum of the individual contributions described in

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**TABLE I.** Summary of systematic uncertainties of the cross section and fragmentation distributions for selected bins in $p_T^{\text{ch jet}}$ and $z^{\text{ch}}$. The contributions from tracking efficiency and track $p_T$ resolution, the event generator dependence of the unfolding correction, MC closure, secondaries correction, UE subtraction and cross section normalization as well as the total uncertainty are shown.

<table>
<thead>
<tr>
<th>Distribution</th>
<th>Bin</th>
<th>Track eff. (%)</th>
<th>Track $p_T$ res. (%)</th>
<th>Event Generator (%)</th>
<th>MC Closure (%)</th>
<th>Sec. corr. (%)</th>
<th>UE (%)</th>
<th>Norm. (%)</th>
<th>Total (%)</th>
</tr>
</thead>
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<td>$\frac{d^2\sigma}{dy dz}$</td>
<td>5–6 GeV/c</td>
<td>7.0</td>
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<td>2.1</td>
<td>...</td>
<td>2.0</td>
<td>1.7</td>
<td>3.5</td>
<td>8.6</td>
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<tr>
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<td>1.0</td>
<td>...</td>
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<td>0.5</td>
<td>3.5</td>
<td>11.1</td>
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<tr>
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<td>86–100 GeV/c</td>
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<td>1.0</td>
<td>3.2</td>
<td>...</td>
<td>5.5</td>
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<td>0.35–0.4</td>
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<td>0.2</td>
<td>2.9</td>
<td>1.0</td>
<td>0.6</td>
<td>...</td>
<td>3.2</td>
<td></td>
</tr>
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<td></td>
<td>0.95–1.0</td>
<td>10.4</td>
<td>0.6</td>
<td>4.7</td>
<td>1.0</td>
<td>0.2</td>
<td>...</td>
<td>11.4</td>
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<td>15–20 GeV/c</td>
<td>0–0.1</td>
<td>4.0</td>
<td>Negligible</td>
<td>0.6</td>
<td>1.0</td>
<td>2.6</td>
<td>...</td>
<td>4.9</td>
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<tr>
<td></td>
<td>0.35–0.4</td>
<td>0.8</td>
<td>0.7</td>
<td>0.9</td>
<td>1.0</td>
<td>0.4</td>
<td>...</td>
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<td>1.0</td>
<td>0.5</td>
<td>...</td>
<td>9.6</td>
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predictions are indicated by shaded bands. The theory systematic uncertainties are related to the choice of scale and PDF as well as the UE subtraction. They are largest at the lowest $p_T^{\text{ch jet}}$ and vary between 25% and 11%. In the jet transverse momentum range $p_T^{\text{ch jet}} > 7 \text{ GeV}/c$, POWHEG+PYTHIA8 (open circles) gives a good description of the data. The spectral shape is reproduced well for $p_T^{\text{ch jet}} > 20 \text{ GeV}/c$. At lower transverse momenta, $5 \leq p_T^{\text{ch jet}} < 20 \text{ GeV}/c$, the calculations overestimate the measured cross section, but the difference is within the combined experimental and theoretical uncertainties. To study the contribution of soft processes generated in PYTHIA8, the POWHEG+PYTHIA8 calculations were repeated with alternative settings, switching off MPI from PYTHIA8. The calculated jet cross sections without MPI (open diamonds) are smaller than the result with default settings in the range $p_T^{\text{ch jet}} < 20 \text{ GeV}/c$, and the measured jet cross section is significantly underpredicted for $p_T^{\text{ch jet}} < 10 \text{ GeV}/c$. The agreement with the data is worse than in the case with MPI. As a further test, we compared the UE activity, measured by the particle $p_T$ density in perpendicular cones, in data and simulations for default and alternative settings. The POWHEG+PYTHIA8 simulations with default settings reproduce the measured UE reasonably well (compare also Ref. [36]), whereas simulations without MPI show a strongly reduced UE $p_T$ density and fail to describe the data. These results indicate a sizable contribution from nonperturbative processes to jet production at

Sec. VI, and are shown as shaded boxes around the data points. The results presented in this work extend the jet $p_T^{\text{ch jet}}$ coverage of previous measurements of the charged jet cross section by the ALICE Collaboration [17], with reduced systematic uncertainties, and are consistent in the common $p_T^{\text{ch jet}}$ range. The previous results are superseded by this work.

The measured charged jet cross sections are compared to calculations from the PYTHIA MC model. The ratios of the MC distributions to measured data are shown in the bottom panel. The systematic uncertainty on the data is indicated by a shaded band drawn at unity. The models qualitatively describe the measured cross sections, but fail to reproduce the spectral shape over the entire range of measured jet $p_T^{\text{ch jet}}$. In the high jet transverse momentum range, $p_T^{\text{ch jet}} > 40 \text{ GeV}/c$ both PYTHIA6 tune Perugia-2011 and PYTHIA8 tune Monash describe the data well, whereas at intermediate $p_T^{\text{ch jet}}$ the jet cross section is systematically overestimated. The discrepancy is about 30–40% for $p_T^{\text{ch jet}} \approx 10–15 \text{ GeV}/c$.

In Fig. 2, the measured cross sections are compared to NLO pQCD calculations with the POWHEG BOX framework, in which the outgoing partons are passed to PYTHIA8 where the subsequent parton shower and hadronization are handled. The UE contribution is subtracted using the method described in Sec. V C in both data and theory calculations. Systematic uncertainties on data and theory calculations are handled. The UE contribution is subtracted using the method described in Sec. VI, and are shown as shaded boxes around the data points. The results presented in this work extend the jet $p_T^{\text{ch jet}}$ coverage of previous measurements of the charged jet cross section by the ALICE Collaboration [17], with reduced systematic uncertainties, and are consistent in the common $p_T^{\text{ch jet}}$ range. The previous results are superseded by this work.

FIG. 1. Top panel: Inclusive charged jet cross section in pp collisions at $\sqrt{s} = 7 \text{ TeV}$ using the anti-$k_T$ algorithm with $R = 0.4$ compared to calculations from PYTHIA6 Perugia-2011 and PYTHIA8 tune Monash. Bottom panel: Ratios of MC distributions to data. The shaded band shows the systematic uncertainty on the data drawn at unity, error bars represent the statistical uncertainties. Most uncertainties are smaller than the marker size.

FIG. 2. Top panel: Inclusive charged jet cross section compared to POWHEG+PYTHIA8 NLO pQCD calculations with and without MPI. In data and calculations, the underlying event contribution is subtracted. Bottom panel: Ratio of POWHEG calculations to data. The shaded bands indicate systematic uncertainties on data and theory predictions.
low $p_T^{ch\ jet}$. Comparing the two settings in the simulations, MPI contribute $\sim50\%$ to the cross section for $5 \leq p_T^{ch\ jet} < 10$ GeV/$c$ and $\sim20\%$ for $p_T^{ch\ jet} \geq 10$ GeV/$c$. In this estimate, a possible additional contribution from initial-state radiation is not taken into account. In a study of low transverse energy clusters in $p\bar{p}$ collisions at $\sqrt{s} = 900$ GeV [47], the contribution from soft processes to jets with $E_T^{\text{low}} > 5$ GeV was evaluated to be $18\%$, similar in magnitude but lower than our estimate. This difference may be attributed to experimental differences in the definition of the jet energy scale and in the theoretical models, but may also reflect the $\sqrt{s}$ evolution of the probability for MPI, represented by the rise of the UE density observed with collision energy [48].

Next-to-leading-order pQCD calculations overestimate the cross sections for inclusive $x^0$ and $\eta$ meson production at midrapidity measured in pp collisions at $\sqrt{s} = 7$ TeV in the $x^0$ ($\eta$) transverse momentum range $0.3 < p_T < 25$ GeV/$c$ ($0.4 < p_T < 15$ GeV/$c$) by up to a factor of 3 [2]. The jet cross section presented in this work covers a $p_T$ range consistent with Ref. [2], and a consistent PDF set was used for the POWHEG calculations. Since the jet cross section observable depends only weakly on the details of parton fragmentation, the good agreement between data and NLO pQCD calculations for jet cross sections suggests the uncertainty in the parton to hadron fragmentation functions to be the cause for the discrepancy observed for neutral mesons.

The left panel of Fig. 3 presents the measured scaled $p_T$ spectra, $F^c$, of charged particles in charged jets reconstructed with a resolution parameter $R = 0.4$. The $F^c$ distributions are shown for four bins in jet $p_T$: $5 \leq p_T^{ch\ jet} < 10$ GeV/$c$, $10 \leq p_T^{ch\ jet} < 15$ GeV/$c$, $15 \leq p_T^{ch\ jet} < 20$ GeV/$c$ and $20 \leq p_T^{ch\ jet} < 30$ GeV/$c$. The spectra span 2 to 3 orders of magnitude. At the lowest $z^{ch}$, for jets with $p_T^{ch\ jet} < 10$ GeV/$c$ the yield increases to a distinct maximum at $z^{ch} \approx 0.05$. This nonmonotonic behavior corresponds to the humpbacked plateau at high values of the variable $\xi = \log(1/z)$ [17,49], which reflects the suppression of low momentum particle production by QCD coherence [50,51]. For jets with $10 \leq p_T^{ch\ jet} < 15$ GeV/$c$ the maximum is less pronounced, and for jets with $15 \leq p_T^{ch\ jet} < 20$ GeV/$c$ the yield is roughly constant for $z < 0.1$. This reflects a shift of the maximum towards lower $z^{ch}$ (corresponding to higher $\xi$) with increasing $p_T^{ch\ jet}$.

A similar $p_T^{ch\ jet}$ dependence was observed in Ref. [17]. For the highest $z^{ch}$ bin, the $F^c$ distributions for jets with $p_T^{ch\ jet} < 20$ GeV/$c$ show a discontinuous increase, which is strongest for the lowest $p_T^{ch\ jet}$ bin. It corresponds to jets with only a single charged constituent, for which $z^{ch} = 1$ by construction. The effect is also observed in the simulations. An increase of the integral of the distributions with $p_T^{ch\ jet}$ is observed, reflecting the rise of particle multiplicity with increasing $p_T^{ch\ jet}$ observed in Ref. [17].

In Ref. [17] it was found that the $F^c$ distributions measured for leading charged jets in the range $p_T^{ch\ jet} \geq 20$ GeV/$c$ are consistent within uncertainties for $z^{ch} > 0.1$, indicating a scaling of charged jet fragmentation with charged jet transverse momentum. For the inclusive charged jet fragmentation distributions in the jet $p_T$ range reported in this work, no such scaling is observed. The shape of the spectra become progressively flatter with

FIG. 3. Left panel: Charged particle scaled $p_T$ spectra $F^c(z^{ch}, p_T^{ch\ jet})$ for different bins in jet transverse momentum. Right panel: Ratio of MC distributions to data. The shaded band shows the systematic uncertainty on the data drawn at unity. Error bars represent the statistical uncertainties.
The measured fragmentation distributions are compared to calculations obtained from the PYTHIA model, and the ratios of the MC distributions to data are presented in the right panel of Fig. 3. The observed trends for the individual tunes are similar for all charged jet $p_T$. The PYTHIA6 tune Perugia-2011 reproduces the fragmentation distributions reasonably well, although there are discrepancies of up to $10\%$ in some kinematic regions. For $p_T^{ch, jet} \geq 10$ GeV/c, the model tends to underpredict the measured yield at high $z^{ch}$. The PYTHIA8 calculations with the Monash tune exhibit a softer spectrum than the data, overpredicting the fragment yield at intermediate $z^{ch} \approx 0.15-0.4$ and underestimating the rates at high $z^{ch}$, the discrepancy reaching $\sim 35\%$ at $z = 1$ for the lowest jet $p_T$ bin. The difference between calculations and data at intermediate $z^{ch}$ is most pronounced at a value of constituent $p_T \approx 2$ GeV/c for all four jet $p_T$ intervals. To investigate the observed differences between data and calculations at higher jet $p_T$, we also compared the leading charged jet $F^c$ distributions in the range $20 \leq p_T^{ch, jet, leading} < 80$ GeV/c from Ref. [17] to PYTHIA simulations. We observe that for $p_T^{ch, jet, leading} \geq 40$ GeV/c the distributions at intermediate $z^{ch}$ are well described, whereas the yield at high $z^{ch}$ is also underestimated for high $p_T^{ch, jet, leading}$.

The data are also compared to the PYTHIA6 Perugia NoCR tune [29]. This tune is an attempt to describe the data sets used for the Perugia tunes without invoking color reconnections (CR) [19] between fragmenting partons to model nonperturbative color string interactions. It does not reproduce the data used to constrain the PYTHIA parameter space well. However, for the $F^c$ distributions reported in this paper, the calculations agree with the data to within about $10\%$. In Ref. [52] it was shown that in the PYTHIA8 model, the effect of CR is strong in events with MPI and increases with MPI activity. Hence, the weak effect of color reconnections on the low-$p_T^{ch, jet}$ fragmentation distributions in PYTHIA may indicate that these jets are dominantly produced in hard scattering events and from MPI with a few hard outgoing partons, rather than being formed as hadron clusters from the fragmentation of many soft partons combined by the jet-finding algorithm.

VIII. SUMMARY

The inclusive charged jet cross section and jet fragmentation distributions at midrapidity in pp collisions at $\sqrt{s} = 7$ TeV were measured. The cross section for a resolution parameter $R = 0.4$ was reported in the $p_T^{ch, jet}$ interval from 5 to 100 GeV/c. We studied charged particle fragmentation in charged jets with $5 \leq p_T^{ch, jet} < 30$ GeV/c, extending the range in Ref. [17]. The integral of the fragmentation distributions increases with jet $p_T$, showing an increase of particle multiplicity in jets. The shapes of the distributions become progressively flatter for lower jet $p_T$.

The measurements were compared to PYTHIA calculations. The cross sections are well described by PYTHIA6 and PYTHIA8 for $p_T^{ch, jet} > 40$ GeV/c. At lower $p_T^{ch, jet}$ the PYTHIA tunes studied here fail to describe the shape of the jet spectra and the cross section is systematically overestimated. PYTHIA6 tune Perugia-2011 gives a reasonable description of the fragmentation distributions, whereas the PYTHIA8 tune Monash exhibits a softer spectrum than the data, with significant deviations particularly at high $z^{ch}$.

The jet cross sections are well described by POWHEG NLO pQCD +PYTHIA8 calculations for the entire measured range of $p_T^{ch, jet}$. The simulations indicate a sizable contribution of multiparton interactions to the jet cross section for low $p_T^{ch, jet}$. We found that PYTHIA6 tune NoCR reproduces the measured fragmentation distributions reasonably well in the entire jet $p_T$ range covered by our measurements, possibly indicating that the contribution of events with multiple soft color connected partons to jet production is small in the kinematic regime of our measurement, $p_T^{ch, jet} > 5$ GeV/c.

The good agreement between the NLO calculations and the measured jet cross section indicates that the previously observed discrepancies between data and NLO calculations of neutral meson production may be due to the fragmentation functions used in these calculations.

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